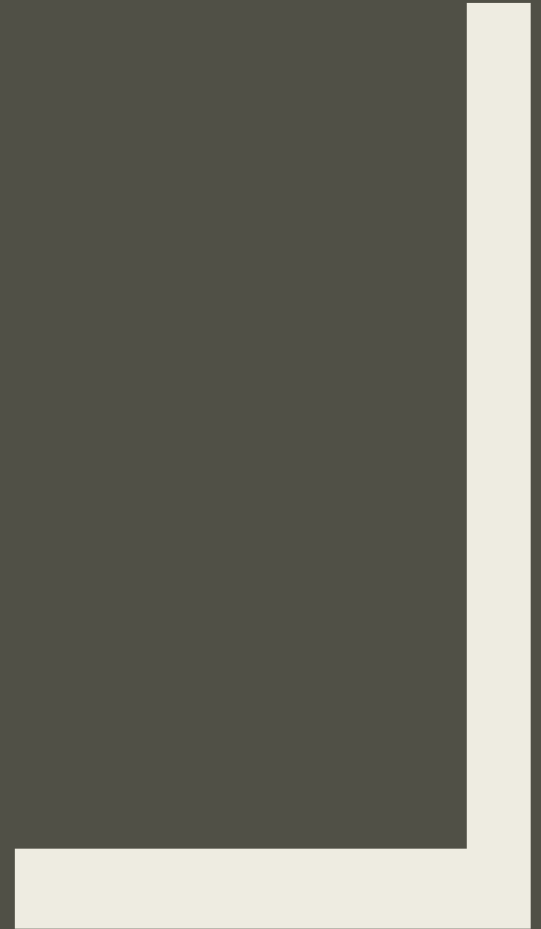


# ARRAYS

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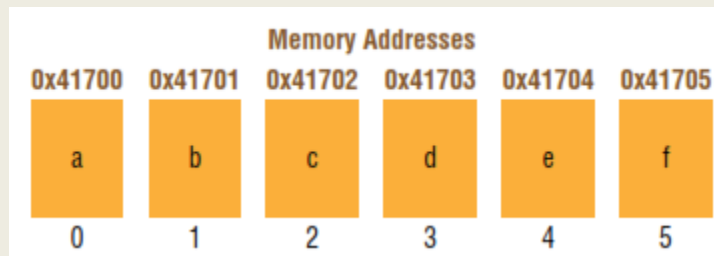
# SUMMARY

- Array Performance
  - Creating an Array
  - Moving Zeros
  - Combining Two Lists
  - Finding the Duplicates in a List
  - Finding the Intersection of Two Lists
- 

# ARRAY

- It is a data structure that stores elements with indexes in a contiguous block of memory.
- This block consists of items stored one after the other in your computer's memory.

homogeneous and static



- A Python list is a heterogeneous variable-length (dynamic) array.
- Different programming languages use different indexing schemes.
  - *Python and C use zero-based indexing*
  - *MATLAB and Fortran, use one-based indexing (the first element is index 1)*

# ARRAY

- The memory location of the first element in an array is called its base address.
- When adding a new item to an array or finding an item in an array.

`base_address + index * size_of_data_type`

- Regardless of whether an array is one-dimensional or multidimensional, your computer stores its elements in a contiguous block of memory.
  - *Access and modify any single element in an array in constant time.*
  - *Searching an unsorted array is  $O(n)$*
  - *Searching an sorted array is  $O(\log n)$*
  - *Modifying the shape of an array, like adding or deleting items is  $O(n)$*

# ARRAY

```
array = [1, 2, 3]
print(array[0])
```

```
array[1] = 'hello'
print(array)
```

```
1
[1, 'hello', 3]
6
```

```
multi_array = [[1, 2, 3], [4, 5, 6], [7, 8, 9]]
print(multi_array[1][2])
```

```
import array
```

```
arr = array.array('f', (1.0, 1.5, 2.0, 2.5))
print(arr[1])
```

```
1.5
```

```
arr[1] = 'hello'
```

```
TypeError: must be real number, not str
```

# ARRAY

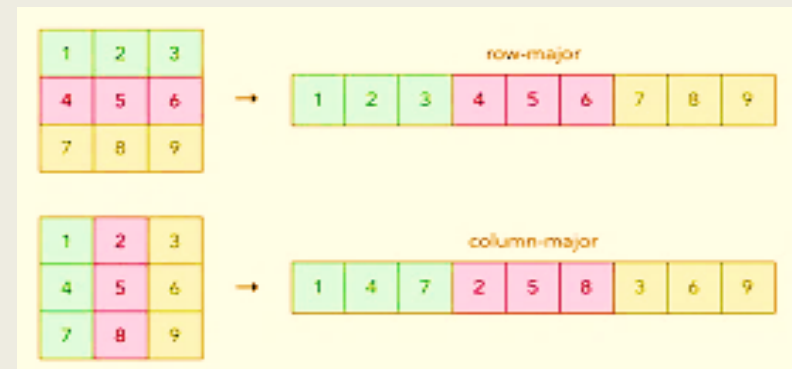
## ■ N-dimensional arrays

- $[[L_1 \dots U_1][\dots][L_n \dots U_n]]$
- Number of elements =  $((U_1 - L_1 + 1) \times \dots \times (U_n - L_n + 1))$
- Memory usage =  $((U_1 - L_1 + 1) \times \dots \times (U_n - L_n + 1)) \times m$

## ■ Two-dimensional arrays are also sometimes called matrices

- $[[L_1 \dots U_1][L_2 \dots U_2]]$
- Number of elements =  $((U_1 - L_1 + 1) \times (U_2 - L_2 + 1))$

## ■ In memory:



# ARRAY

- A triangular matrix is a special type of square matrix where all of the elements above or below the main diagonal are zero.

Upper Triangular Matrix

$$\begin{pmatrix} a & b & c \\ 0 & d & e \\ 0 & 0 & f \end{pmatrix}$$

Lower Triangular Matrix

$$\begin{pmatrix} a & 0 & 0 \\ b & c & 0 \\ d & e & f \end{pmatrix}$$

$$A[i, j] = 0 \quad i < j$$

$$A[i, j] = 0 \quad i > j$$

$$\begin{bmatrix} 1 & 6 & 7 \\ 0 & 2 & 5 \\ 0 & 0 & 4 \end{bmatrix} \implies \begin{array}{|c|c|c|c|c|c|} \hline & 1 & 2 & 3 & 4 & 5 & 6 \\ \hline 1 & 6 & 2 & 7 & 5 & 4 \\ \hline \end{array}$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 2 & 5 & 0 \\ 3 & 1 & 1 \end{bmatrix} \implies \begin{array}{|c|c|c|c|c|c|} \hline & 1 & 2 & 3 & 4 & 5 & 6 \\ \hline 1 & 2 & 5 & 3 & 1 & 1 \\ \hline \end{array}$$

# ARRAY

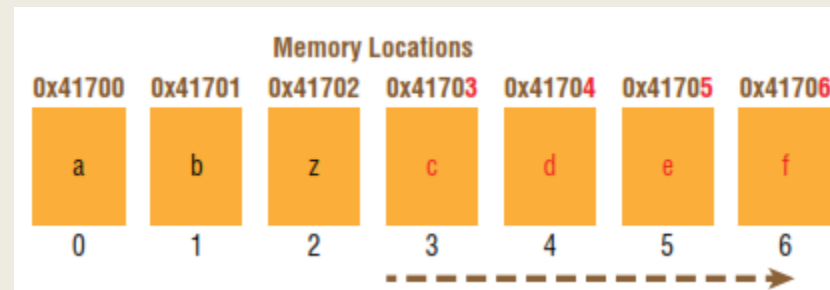
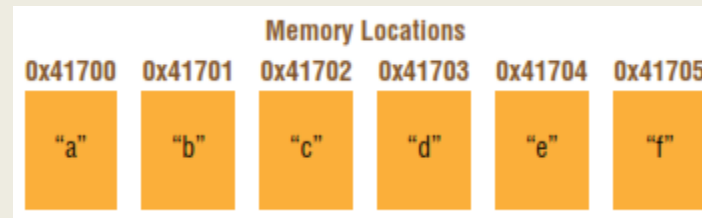
- Sparse matrix:

|   |   |   |   |   |   |
|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 9 | 0 |
| 0 | 8 | 0 | 0 | 0 | 0 |
| 4 | 0 | 0 | 2 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 5 |
| 0 | 0 | 2 | 0 | 0 | 0 |



| Rows | Columns | Values |
|------|---------|--------|
| 5    | 6       | 6      |
| 0    | 4       | 9      |
| 1    | 1       | 8      |
| 2    | 0       | 4      |
| 2    | 3       | 2      |
| 3    | 5       | 5      |
| 4    | 2       | 2      |

# ARRAY



- This problem is worse for static arrays because your computer can't guarantee the memory addresses that come after the memory block it reserved for the array are free.
  - *C reserves a new block of memory for the array, copy all the items from the old block to the new one, add the new element, and then free the old block.*
  - *Python uses overallocation: reserving more memory for an array than it needs.*

# ARRAY

## ■ Summation:

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} + \begin{bmatrix} e & f \\ g & h \end{bmatrix} = \begin{bmatrix} a+e & b+f \\ c+g & d+h \end{bmatrix}$$

A                      B                      C

## ■ Complexity:

$O(n \times m)$  or  $O(n^2)$

```
for i = 1 to n
  for j = 1 to n
    cij = aij + bij
```

# ARRAY

## ■ Multiplication:

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} \times \begin{bmatrix} e & f \\ g & h \end{bmatrix} = \begin{bmatrix} ae + bg & af + bh \\ ce + dg & cf + dh \end{bmatrix}$$

A                      B                      C

## ■ Complexity:

$O(n \times m \times p)$  or  $O(n^3)$

```
for  $i = 1$  to  $n$ 
  for  $j = 1$  to  $n$ 
     $c_{ij} = 0$ 
    for  $k = 1$  to  $n$ 
       $c_{ij} = c_{ij} + a_{ik} \cdot b_{kj}$ 
```

# ARRAY

## ■ Transpose:

$$\begin{bmatrix} 3 & 4 \\ 2 & 1 \end{bmatrix} = \begin{bmatrix} 3 & 2 \\ 4 & 1 \end{bmatrix}$$

Input Matrix                  Transpose Matrix

## ■ Complexity:

$O(n \times m)$  or  $O(n^2)$

```
for i = 1 to n
  for j = 1 to n
    bji = aij
```

# MOVING ZEROS

- Challenge: locate all the zeros in a list and push them to the end, leaving the remaining elements in their original order.

```
[8, 0, 3, 0, 12]
```

```
[8, 3, 12, 0, 0]
```

```
def move_zeros(a_list):
    zero_index = 0
    for index, n in enumerate(a_list):
        if n != 0:
            a_list[zero_index] = n
            if zero_index != index:
                a_list[index] = 0
            zero_index += 1
    return(a_list)

a_list = [8, 0, 3, 0, 12]
move_zeros(a_list)
print(a_list)
```

# COMBINING TWO LISTS

## ■ Challenge:

```
movie_list = [ "Interstellar", "Inception",  
               "The Prestige", "Insomnia",  
               "Batman Begins"  
             ]
```

```
[('Interstellar', 1),  
 ('Inception', 10),  
 ('The Prestige', 10),  
 ('Insomnia', 8),  
 ('Batman Begins', 6)]
```

```
ratings_list = [1, 10, 10, 8, 6]
```

```
movie_list = [ "Interstellar", "Inception",  
               "The Prestige", "Insomnia",  
               "Batman Begins"  
             ]
```

```
ratings_list = [1, 10, 10, 8, 6]
```

```
print(list(zip(movie_list, ratings_list)))
```

# FINDING THE DUPLICATION IN A LIST

- Challenge: check for duplicate items in a list, which you will also have to do often in real- world programming.
  - *Comparing every item to every other item,  $O(n**2)$*
  - *Using Python **set**.*

```
a_set = set()
a_set.add("Kanye West")
a_set.add("Kendall Jenner")
a_set.add("Justin Bieber")
print(a_set)

a_set.add('Kanye West')
print(a_set)
```

```
{'Justin Bieber', 'Kanye West', 'Kendall Jenner'}
{'Justin Bieber', 'Kanye West', 'Kendall Jenner'}
```

# FINDING THE DUPLICATION IN A LIST

```
def duplicates(an_iterable):  
    dups = []  
    a_set = set()  
    for item in an_iterable:  
        l1 = len(a_set)  
        a_set.add(item)  
        l2 = len(a_set)  
        if l1 == l2:  
            dups.append(item)  
    return dups
```

```
a_list = [  
    'Susan Adams',  
    'Kwame Goodall',  
    'Jill Hampton',  
    'Susan Adams']
```

```
dups = duplicates(a_list)  
print(dups)
```

['Susan Adams']

# FINDING THE INTERSECTION OF TWO LISTS

## ■ Challenge:

```
this_weeks_winners = [2, 43, 48, 62, 64, 28, 3]
most_common_winners = [1, 28, 42, 70, 2, 10, 62, 31, 4, 14]
```

```
[2, 62, 28]
```

```
def return_inter(list1, list2):
    list3 = [v for v in list1 if v in list2]
    return list3
```

```
list1 = [2, 43, 48, 62, 64, 28, 3]
list2 = [1, 28, 42, 70, 2, 10, 62, 31, 4, 14]
print(return_inter(list1, list2))
```

```
[2, 62, 28]
```

```
def return_inter(list1, list2):
    set1 = set(list1)
    set2 = set(list2)
    return list(set1.intersection(set2))
```

```
list1 = [2, 43, 48, 62, 64, 28, 3]
list2 = [1, 28, 42, 70, 2, 10, 62, 31, 4, 14]
new_list = return_inter(list1, list2)
print(new_list)
```

```
[2, 28, 62]
```